

# Thermodynamic Evaluation of the Si-C-Al-Y-O System for LPS-SiC Application

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**A thermodynamic dataset for the Si-C-Al-Y-O system was developed for calculations of heterogeneous phase equilibria and reactions in SiC-base engineering ceramics. The quinary system is of major interest for the understanding of the liquid phase sintering of silicon carbide ceramics using additives like alumina ( $\text{Al}_2\text{O}_3$ ) and yttria ( $\text{Y}_2\text{O}_3$ ). The thermodynamic dataset was developed by the CALPHAD method of thermodynamic optimization. Analytical descriptions for the Gibbs free energy functions of all phases in the Si-C-Al-Y-O system were assessed. The sublattice model using the compound energy formalism was used for the treatment of the solid phases. The liquid phase was described by using the partially ionic liquid model presented as  $(\text{Al}^{3+}, \text{Si}^{4+}, \text{Y}^{3+})_P(\text{O}^{2-}, \text{SiO}_4^{4-}, \text{Va}, \text{AlO}_{3/2}, \text{SiO}_2, \text{C})_Q$ , which covers metallic liquid and oxide liquid as a single phase.**

**Keywords** LPS-SiC, phase diagram, Si-C-Al-Y-O system, thermodynamic modeling

## 1. Introduction

Silicon carbide (SiC) is one of the promising structural materials for mechanical and thermal applications because of its excellent properties, with regard to strength, hardness, chemical stability, wear and oxidation resistance, high thermal conductivity, creep and thermal shock.<sup>[1,2]</sup> It is also a promising inert matrix fuel material for irradiation of plutonium and minor actinides because of its irradiation damage tolerance.<sup>[3-6]</sup>

The sintering of SiC is usually performed at very high temperatures up to 2200 °C in the solid state (SSiC), with small amounts of boron, carbon, or aluminium as additives because of the strong Si-C bond and low self-diffusion coefficients. In the 1980s liquid phase sintered silicon carbide LPSSiC was developed as a material with higher fracture toughness than the SSiC but with a similar hardness. Sintering additives like  $\text{Y}_2\text{O}_3/\text{Al}_2\text{O}_3$ , AlN or other rare earths form a liquid phase at remarkably lower temperatures thus allowing a reduction of the sintering temperature. The additives crystallize during cooling and mostly form rare earth aluminates especially of garnet structure ( $\text{YAG}$ ,  $\text{Y}_3\text{Al}_5\text{O}_{12}$ ).<sup>[7-15]</sup>

The oxygen content of SiC powder, existing either as surface  $\text{SiO}_2$  or as interstitial oxygen is between 0.8 and 1.1 wt.%  $\text{SiO}_2$ .<sup>[16-21]</sup> Surface  $\text{SiO}_2$  is detrimental to the solid state sintering of SiC because gas evolution at the SiC/ $\text{SiO}_2$  interface can cause the destruction of inter-particle connects

and lead to excessive porosity in the final specimen.<sup>[21]</sup> Weight loss and microstructure development studies during liquid phase sintering with  $\text{Al}_2\text{O}_3$ - $\text{Y}_2\text{O}_3$  additives as well as thermodynamic calculations were performed by Grande et al.<sup>[16]</sup> It should be mentioned that, in the case of liquid phase sintering, surface  $\text{SiO}_2$  can react with the sintering additives  $\text{Al}_2\text{O}_3$  and  $\text{Y}_2\text{O}_3$  and form an oxide liquid phase at even lower temperatures than the oxide liquid phase produced by reactions between  $\text{Al}_2\text{O}_3$  and  $\text{Y}_2\text{O}_3$  alone.<sup>[20]</sup> For example, although the lowest eutectic temperature in the  $\text{Al}_2\text{O}_3$ - $\text{SiO}_2$  pseudo-binary system is at 2083 K,<sup>[20]</sup> Mulla et al. reported liquid phase formation at about 2033 K<sup>[17]</sup> and Lee et al. showed sudden densification of SiC with  $\text{Al}_2\text{O}_3$  and  $\text{Y}_2\text{O}_3$  additives at 1773 K.<sup>[9]</sup> However, during liquid phase sintering  $\text{SiO}_2$ ,  $\text{Y}_2\text{O}_3$  and  $\text{Al}_2\text{O}_3$  react with SiC resulting in gaseous CO,  $\text{SiO}$ ,  $\text{Al}_2\text{O}$  and Al. These interactions cause weight losses, porosity and the formation of sintering skins or even instabilities of the materials.<sup>[22-28]</sup>

The understanding of the sintering and microstructure formation in these materials is the preposition of their reproducible production. Computational thermodynamics can support the understanding and modeling of reactions and process described above Ref 22, 26. The aim of present paper is to review available experimental and thermodynamic data for the relevant systems and to develop thermodynamic database for application of SiC liquid phase sintering.

## 2. Thermodynamic Data of the System

Several research groups contributed to derive thermodynamic parameters for the  $\text{Y}_2\text{O}_3$ - $\text{Al}_2\text{O}_3$ - $\text{SiO}_2$  system. Fabrichnaya et al.<sup>[29]</sup> assessed the  $\text{Y}_2\text{O}_3$ - $\text{Al}_2\text{O}_3$ - $\text{SiO}_2$  system and its subsystems based on available experimental phase diagrams and calorimetric measurements of solid phases. They described the liquid phase with the ionic two-sublattice model using the formula  $(\text{Y}^{3+})_P(\text{O}^{2-}, \text{SiO}_4^{4-}, \text{AlO}_{1.5}, \text{SiO}_2)_Q$ . Later Mao et al.<sup>[30]</sup> re-assessed thermodynamic properties in the

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$\text{Y}_2\text{O}_3\text{-Al}_2\text{O}_3\text{-SiO}_2$  ternary system and its constituent binaries  $\text{Y}_2\text{O}_3\text{-Al}_2\text{O}_3$  and  $\text{Y}_2\text{O}_3\text{-SiO}_2$  using different species in the model of ionic liquid than Fabrichnaya et al.<sup>[29]</sup> The liquid phase was described by the ionic two-sublattice model with the formula  $(\text{Al}^{3+}, \text{Y}^{3+})_P(\text{AlO}_2^{1-}, \text{O}^{2-}, \text{SiO}_4^{4-}, \text{SiO}_2^0)_Q$ . With this model, the liquid miscibility gap in the  $\text{SiO}_2$  rich part of ternary system can be reproduced better than in the work of Fabrichnaya et al.<sup>[29]</sup> However, the deviations from experimental data for invariant reactions were large in work of Mao et al.<sup>[30]</sup> (see Table 1). Mao et al.<sup>[30]</sup> considered two versions of database. According to calculations with dataset-1, which the authors<sup>[30]</sup> gave some preference, the  $\text{Y}_2\text{Si}_2\text{O}_7$  phase in  $\text{Y}_2\text{O}_3\text{-SiO}_2$  binary system melts congruently contradicting experimental data. For the description of liquid phase sintering, the  $\text{SiO}_2$ -rich part of phase diagram is not very important, because silica content on SiC surface does not exceed 2 mass%. Based on this consideration, the dataset of Fabrichnaya et al.<sup>[29]</sup> was accepted as the starting point in this work for further re-assessment using the same thermodynamic models for phases as in Fabrichnaya et al.<sup>[29]</sup> Additionally, the comparison of results for the  $\text{Si}_3\text{N}_4\text{-AlN-Al}_2\text{O}_3\text{-SiO}_2$  system obtained by Dumitrescu and Sundman<sup>[31]</sup> with recent assessment of Mao et al.<sup>[32]</sup> did not reveal any advantage of using ionic liquid model with  $\text{AlO}_2^{1-}$  species.

Thermodynamic database for the  $\text{Y}_2\text{O}_3\text{-Al}_2\text{O}_3\text{-SiO}_2$  system of Ref 29 was incorporated into the database for the Al-C-O-Si-Y system<sup>[33]</sup> by Cupid et al.<sup>[34]</sup> Calculations were performed by Cupid et al.<sup>[34]</sup> to explore some aspects of the thermodynamics of liquid phase sintering of SiC with  $\text{Al}_2\text{O}_3$  and  $\text{Y}_2\text{O}_3$  additives. However, in the work of Cupid et al.<sup>[34]</sup> two different descriptions of liquid were used, for metallic liquid and ionic oxide liquid. In the Y-O rich compositions,

such simplification cannot be accepted, because in the Y-O system the liquid phase continuously dissolves oxygen and certainly does not decompose into two liquid phases.

Recently, the thermodynamic description of yttrium was updated and recommended by the Scientific Group Thermodata Europe.<sup>[35]</sup>

Therefore, the aim of this work was the development of a self-consistent thermodynamic database for the Al-Si-Y-C-O system which can be used for modelling of liquid phase sintering of SiC. All systems including yttrium should be updated, checked for consistency with experimental data and re-assessed if necessary. Two-sublattice partially ionic liquid model describing the liquid phase in wide composition ranges from metallic liquid to oxide ionic liquid and finally to highly polymerized  $\text{SiO}_2$  liquid should be incorporated.

### 3. Thermodynamic Modeling

The CALPHAD (CALculation of PHase Diagrams) method<sup>[36,37]</sup> was used to determine phase equilibria and phase reactions in the multi-component systems. Unary data for the pure elements<sup>[38]</sup> and descriptions of gaseous species were taken from the SGTE substance database.<sup>[35]</sup> Thermodynamic description of Al-C, Al-O, Al-Si, C-Si, C-O and Si-O binary systems were taken from SGTE database (SSOL, solution database and SSUB, substance database see Ref 35). The Al-Y,<sup>[39]</sup> C-Y<sup>[40]</sup> and Si-Y<sup>[41]</sup> systems were updated by Lukas using new pure yttrium SGTE-data for publication in Landolt-Börnstein series. These results were also adopted in present work. Recently new thermodynamic

**Table 1** Invariant phase equilibria including the liquid phase in the  $\text{Y}_2\text{O}_3\text{-Al}_2\text{O}_3\text{-SiO}_2$  system

Solid phases in equilibrium with the liquid phase	Temperature, K	Comparison of equilibrium conditions between experiments and assessments	
		Liquid composition, mass%	
		$\text{Al}_2\text{O}_3$	$\text{SiO}_2$
$\text{Y}_2\text{O}_3\text{R} + \text{Y}_2\text{SiO}_5 + \text{YAM}$	2113(a) (2018) <2060> {2031}	8.5(a) (4.7) <5.4> {8.8}	11.0(a) (10.2) <8.6> {9.3}
$\text{Mul} + \text{Tri} + \gamma - \text{Y}_2\text{Si}_2\text{O}_7$	1618(a), 1644(b) (1558) <1620> {1625}	22.0(a), 25.1(b) (20.3) <20.6> {21.7}	46.0(a), 44.2(b) (47.7) <54.8> {47.6}
$\text{Y}_2\text{SiO}_5 + \text{YAM} + \text{YAG}$	(1961) <2018> {1908}	(16.9) <20.1> {21.1}	(12.6) <10.0> {11.6}
$\text{YAM} + \text{YAP} + \text{YAG}$	(1966) <2020> {1919}	(16.9) <20.2> {21.3}	(12.4) <9.8> {10.8}
$\text{Mul} + \text{Al}_2\text{O}_3 + \gamma - \text{Y}_2\text{Si}_2\text{O}_7$	(1630) <1715> {1685}	(24.5) <24.4> {24.0}	(33.5) <40.0> {38.2}
$\text{Y}_2\text{SiO}_5 + \text{YAG} + \gamma - \text{Y}_2\text{Si}_2\text{O}_7$	(1706) <1851> {1737}	(20.9) <36.1> {24.1}	(24.1) <20.8> {24.0}
$\text{YAG} + \text{Al}_2\text{O}_3 + \gamma - \text{Y}_2\text{Si}_2\text{O}_7$	(1671) <1813> {1733}	(23.6) <40.6> {25.1}	(24.3) <19.9> {24.2}
$\text{Cri} + \text{Tri} + \text{Mul}$	(1744) <1744> {1744}	(15.0) <12.2> {24.8}	(72.8) <80.9> {51.5}
$\text{Cri} + \text{Tri} + \gamma - \text{Y}_2\text{Si}_2\text{O}_7$	(1744) <1744> {1744}	(10.4) <14.7> {15.3}	(55.4) <55.4> {49.5}
$\text{Cri} + \delta + \gamma - \text{Y}_2\text{Si}_2\text{O}_7$	(1854) <1854> {1854}	(4.8) <8.0> {9.7}	(51.1) <48.8> {49.8}
$\text{Y}_2\text{SiO}_5 + \delta + \gamma - \text{Y}_2\text{Si}_2\text{O}_7$	(1854) <1854> {1854}	(12.2) <35.2> {16.8}	(26.9) <21.2> {27.3}

Data in ( ) and < > are calculated according to the dataset 1 and dataset 2 after Ref 32 in the present work, respectively. Those in { } are calculated in this study

(a) Experimental data from Ref 70  
(b) Experimental data from Ref 71

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descriptions of the Al-Y and Y-Si have been published by Liu et al.<sup>[42]</sup> and Shukla et al.<sup>[43]</sup> respectively. The calculated phase diagram of Al-Y system and thermodynamic properties in work of Liu et al.<sup>[42]</sup> reproduces available experimental data with the same uncertainty as updated description of Lukas.<sup>[39]</sup> The results obtained with both descriptions are very similar to each other and therefore SGTE recommendation was accepted. It should be mentioned that the description of Shukla et al.<sup>[43]</sup> for Y-Si system can not be directly used in present study because different thermodynamic model (quasi-chemical) was used there.

Thermodynamic data from the  $\text{Al}_2\text{O}_3\text{-SiO}_2$  quasibinary system were accepted from work of Dumitrescu and Sundman.<sup>[31]</sup>

The liquid phase is described by the partially ionic sublattice model, presented by a formula  $(\text{Al}^{3+}, \text{Si}^{4+}, \text{Y}^{3+})_P(\text{O}^{2-}, \text{SiO}_4^{4-}, \text{Va}, \text{AlO}_{3/2}, \text{SiO}_2, \text{C})_Q$ . The Gibbs energy is expressed by equation:

$$G_M = \sum_C \sum_A y_C y_A {}^0 G_{C:A} + Q y_{\text{Va}} \sum_C y_C {}^0 G_C + Q \sum_N y_N {}^0 G_N + RT \left[ P \sum_C y_C \ln(y_C) + Q \left( \sum_A y_A \ln(y_A) + y_{\text{Va}} \ln(y_{\text{Va}}) + \sum_N y_N \ln(y_N) \right) \right] + {}^E G_M \quad (\text{Eq 1})$$

where  $P$  and  $Q$  are stoichiometric factors changing with composition. The subscripts C, A, Va, and N denote cations, anions, vacancies, and neutral species respectively, and  $y_i$  is the site fraction of species  $i$  on a given sublattice.  ${}^E G_M$  is the excess Gibbs energy derived from binary and higher order interactions. The stoichiometric coefficients  $P$  and  $Q$  are defined as

$$Q = \sum_C v_C y_C \quad (\text{Eq 2})$$

$$P = \sum_A (-v_A) y_A + Q y_{\text{Va}} \quad (\text{Eq 3})$$

where  $v_i$  is the charge on species  $i$ .

Vacancies were included in the anionic sub-lattice as well as carbon to describe metallic liquid. It should be mentioned that in some sub systems, like Al-O, the liquid phase has a wide miscibility gap separating metallic and oxide liquids, while in the other systems, i.e. in the Y-O binary system, there is no miscibility gap. Therefore it is important to have a single phase description for liquid to cover these different cases.

Except for the mullite and YAM (monoclinic yttrium aluminate phase,  $\text{Y}_4\text{Al}_2\text{O}_9$ ) phases, all the solid phases in the  $\text{Y}_2\text{O}_3\text{-Al}_2\text{O}_3\text{-SiO}_2$  ternary system are treated as stoichiometric compounds. Four modifications ( $\alpha, \beta, \gamma, \delta$ ) of  $\text{Y}_2\text{Si}_2\text{O}_7$  phase were considered. For the  $\text{Y}_2\text{SiO}_5$  only the B modification is considered due to lack of data for the A modification. Two yttria modifications,  $\text{Y}_2\text{O}_3\text{-R}$  (cubic C-type) and  $\text{Y}_2\text{O}_3\text{-H}$  (hexagonal), are considered and narrow homogeneity ranges in these phases were modelled by sublattice model. Three modifications of silica cristobalite, tridymite and quartz were described as stoichiometric compounds. The homogeneity range in mullite phase and  $\text{SiO}_2$  solubility in the YAM phase were modelled by a

sublattice model in the form of compound energy formalism.<sup>[44]</sup> The Gibbs energy of these phases is given by:

$$G_M = \sum_J \Delta_f {}^0 G_{\text{end}} \Pi y_J^S + RT \sum_S \sum_J n_J^S y_J^S \ln(y_J^S) + {}^E G_M \quad (\text{Eq 4})$$

where S and J denote the sublattice and species, respectively, and  ${}^0 G_{\text{end}}$  is the Gibbs energy of the end members.

The sublattice model was also used to describe homogeneity ranges in several phases in the Al-C-O-Si-Y system. Terminal solutions fcc, bcc, hcp and diamond were described by a two sublattice model. Solubility of Si in the  $\text{Al}_4\text{C}$  phase, solubility of O and C in the  $\text{Y}_5\text{Si}_3$  phase, homogeneity range in the  $\text{Y}_2\text{C}_3$  phase in the Y-C system, homogeneity range in the  $\gamma$ -phase in the Y-C binary and solubility of O in  $\gamma$ -phase were also modelled by a sublattice model.<sup>[33]</sup>

## 4. Thermodynamic Optimizations

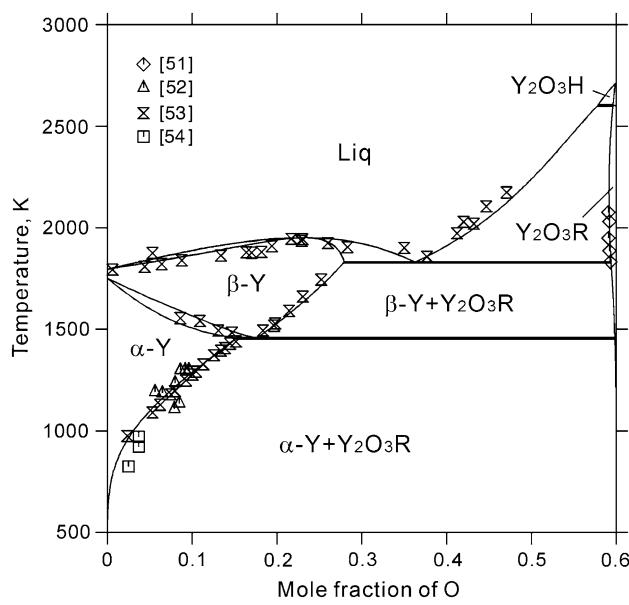
For the optimization of thermodynamic parameters and calculation of phase diagrams, the THERMO-CALC program package was used.<sup>[45]</sup> Thermodynamic parameters assessed by this work are listed in Table 2.

**Table 2 Thermodynamic parameters assessed by this work**

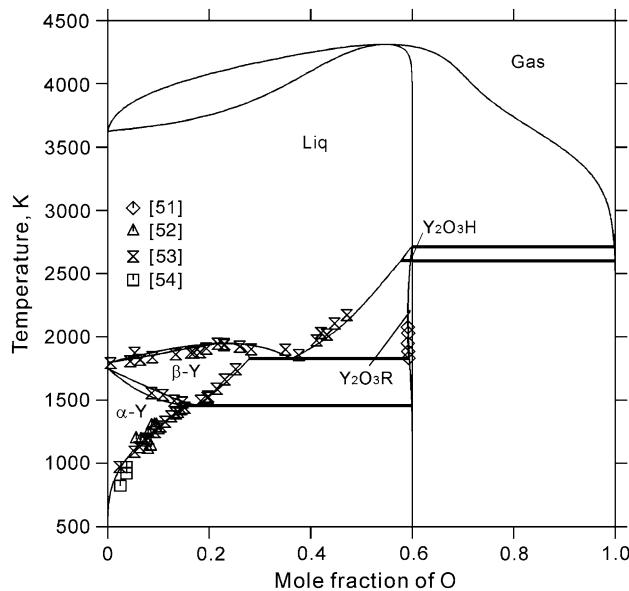
Liquid $(\text{Al}^{3+}, \text{Si}^{4+}, \text{Y}^{3+})_P(\text{O}^{2-}, \text{SiO}_4^{4-}, \text{Va}, \text{AlO}_{3/2}, \text{SiO}_2, \text{C})_Q$		
$\text{Y}^{3+}(\text{O}^{2-}, \text{Va})$	$L^0$	$238524 - 134.7162 * T$
$\text{Y}^{3+}(\text{O}^{2-}, \text{SiO}_2)$	$L^0$	$84910 - 101.2572 * T$
$\text{Y}^{3+}(\text{O}^{2-}, \text{SiO}_2)$	$L^1$	$-570136 + 178.1970 * T$
$\text{Y}^{3+}(\text{O}^{2-}, \text{SiO}_4^{4-}, \text{AlO}_{3/2})$	$L^0$	$-2412716$
$\text{Y}^{3+}(\text{SiO}_4^{4-}, \text{AlO}_{3/2})$	$L^0$	$848816 + 54.60616 * T$
$\text{Y}^{3+}(\text{SiO}_4^{4-}, \text{AlO}_{3/2})$	$L^1$	$524377$
$\text{Y}^{3+}(\text{SiO}_4^{4-}, \text{AlO}_{3/2}, \text{SiO}_2)$	$L^0$	$-2976431$
Bcc $(\text{Si}, \text{Y})(\text{C}, \text{O}, \text{Va})_3$		
$\text{Y}: \text{O}$	$L^0$	$-158000 + 114.1952 * T$
$\text{Y}(\text{O}, \text{Va})$	$L^0$	$-2342689 + 98.2777 * T$
$\text{Y}(\text{O}, \text{Va})$	$L^1$	$-764174$
Hcp $(\text{Al}, \text{Si}, \text{Y})(\text{C}, \text{O}, \text{Va})$		
$\text{Y}: \text{O}$	$L^0$	$-592135 + 73.5098 * T$
$\text{Y}(\text{O}, \text{Va})$	$L^0$	$3500$
Gamma $\text{Y}(\text{C}, \text{C}_2\text{O}, \text{Va})$		
$\text{Y}(\text{C}, \text{O})$	$L^0$	$-200000$
$\text{Y}(\text{C}, \text{O})$	$L^1$	$100000$
YAM $(\text{Al}^{3+}, \text{Si}^{4+})_2(\text{Y}^{3+})_4(\text{O}^{2-}, \text{Va})(\text{O}^{2-})_9$		
$(\text{Al}^{3+}, \text{Si}^{4+})\text{Y}^{3+}\text{O}^{2-}\text{O}^{2-}$	$L^0$	$760241 + 9.998 * T$
$\text{Al}^{3+}\text{Y}^{3+}(\text{O}^{2-}, \text{Va})\text{O}^{2-}$	$L^0$	$-336375 + 132.586 * T$
$\text{Si}^{4+}\text{Y}^{3+}(\text{O}^{2-}, \text{Va})\text{O}^{2-}$	$L^0$	$-417660 - 258.293 * T$
$(\text{Al}^{3+}, \text{Si}^{4+})\text{Y}^{3+}\text{VaO}^{2-}$	$L^0$	$-236373 + 122.137 * T$
$\gamma\text{-Y}_2\text{Si}_2\text{O}_7$		
$\text{Y}_2\text{Si}_2\text{O}_7$	$G^0$	$-3925077 + 1591.0739 * T$
		$-264.23561 * T * \ln T$
		$-0.0129019088 * T^2 + 3559383/T$
$\text{Y}_2\text{SiO}_5$		
$\text{Y}_2\text{SiO}_5$	$G^0$	$-2963134 + 1057.602 * T$
		$-181.294814 * T * \ln T$
		$-0.0110113475 * T^2 + 1803501/T$

#### 4.1 Y-O Binary System

The Y-O binary system was re-optimized in this work. For the optimization, phase diagram data and thermo-chemical properties of the different phases of the system were used. The Y-O system contains the following phases:  $\alpha$ -yttrium,  $\beta$ -yttrium,  $\text{Y}_2\text{O}_3\text{-R}$ ,  $\text{Y}_2\text{O}_3\text{-H}$ , Y-O liquid, and gas.  $\alpha$ -Yttrium (hcp structure) is stable up to 1751 K, where it transforms into  $\beta$ -yttrium (bcc structure).  $\beta$ -Yttrium melts at 1795 K. Both  $\alpha$ -Y and  $\beta$ -Y can

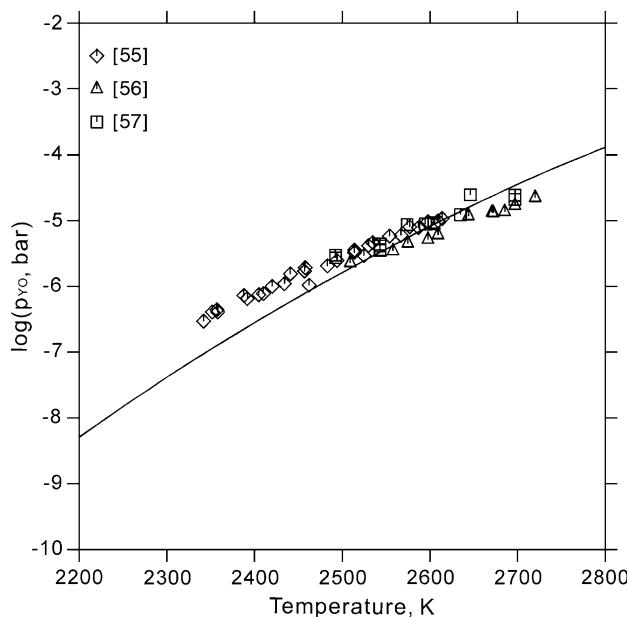


**Fig. 1** The calculated Y-O phase diagram compared with experimental data

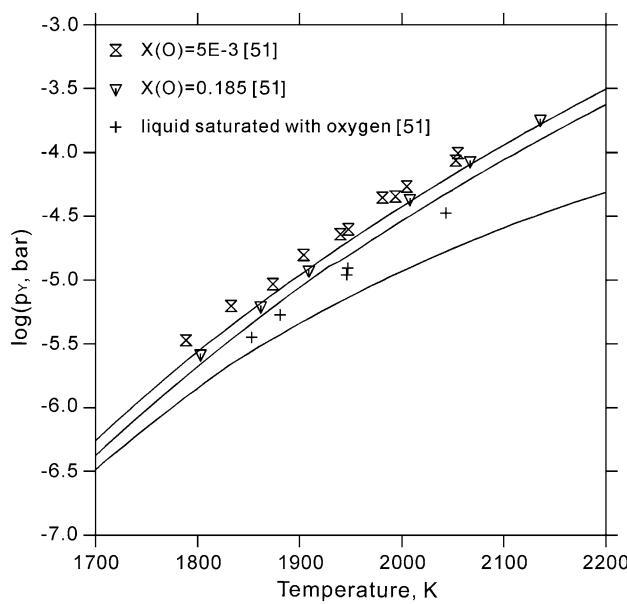


**Fig. 2** The calculated Y-O phase diagram up to high temperatures

dissolve considerable amounts of oxygen in their structure. Thermodynamic evaluations of the Y-O system have been published by Gröbner,<sup>[33]</sup> Ran et al.,<sup>[46]</sup> Lysenko<sup>[47]</sup> and Swamy et al.<sup>[48]</sup> All four evaluations have used essentially the same thermodynamic models to describe the condensed solution phases; those originally adopted by Ran et al.,<sup>[46]</sup> while they differ with regard to the experimental data used. The solubility of oxygen in  $\alpha$ - and  $\beta$ -yttrium modifications was described as



**Fig. 3** The calculated equilibrium  $\text{YO}(\text{g})$  pressures over  $\text{Y}_2\text{O}_3$  compared with experimental data



**Fig. 4** The calculated equilibrium yttrium pressures over the liquid compared with experimental data

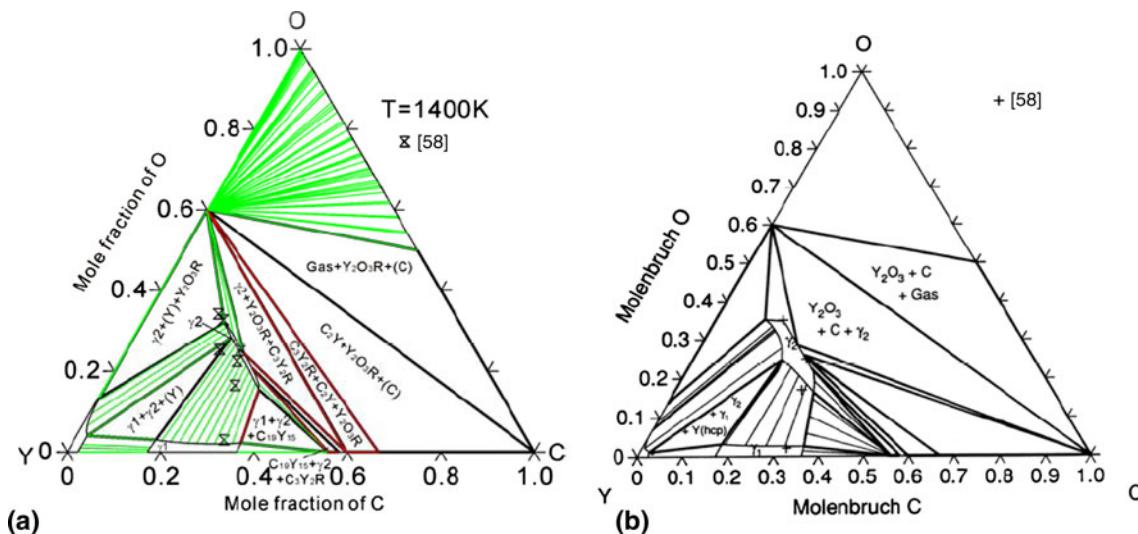
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interstitial solution by sublattice model. The Wagner-Schottky model in the form of sublattice model was used to describe the small deviation from the stoichiometry of  $\alpha$ -yttria ( $\text{Y}_2\text{O}_3\text{-R}$ ) and the same model was applied to the high-temperature polymorph,  $\beta$ -yttria ( $\text{Y}_2\text{O}_3\text{-H}$ ). Recently new assessment of Djurovic et al.<sup>[49]</sup> has been published. They used a model for bcc phase which was different from SGTE recommendation. Their model of  $\text{Y}_2\text{O}_3$  phases was selected to make it consistent with  $\text{ZrO}_2\text{-Y}_2\text{O}_3$  description. The existence of  $\text{Y}^{2+}$  ions assumed by Djurovic et al.<sup>[49]</sup> is experimentally not established. In the present study, the phase models were selected the same as in work of Swamy et al.<sup>[48]</sup> Thermodynamic parameters of the  $\text{Y}_2\text{O}_3$  modifications were accepted from Zinkevich.<sup>[50]</sup>

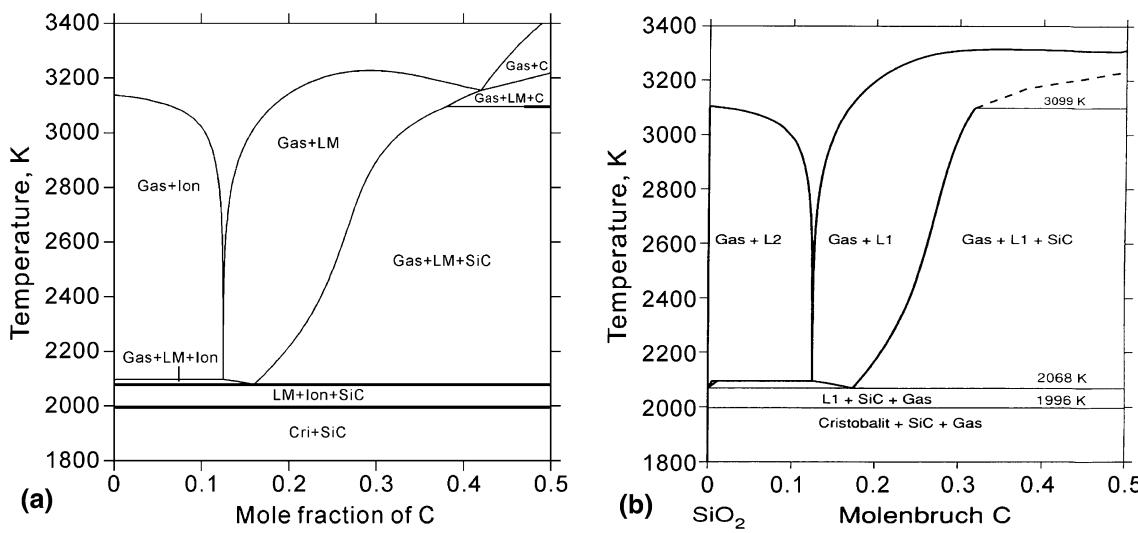
Calculated Y-O binary phase diagrams are shown in Fig. 1 along with experimental data.<sup>[51-54]</sup> The experimental solvus,

solidus, and liquidus relations are very well reproduced by calculation. Also, the calculated eutectoid and eutectic reactions are consistent with the experimental data. Special care was taken in the Y-rich side at high temperature, because if description of Swamy et al.<sup>[48]</sup> is used in combination with gas description from SGTE (SSUB database) the  $\text{Y}_2\text{O}_3\text{-H}$  phase will appear stable at high temperatures in the Y-rich composition range according to calculations. As shown in Fig. 2, the present thermodynamic data set gives reasonable predictions at temperatures above 3500 K, and thus, adequately describes the phase relations in the Y-O system in wide range of temperatures and compositions.

Thermodynamic data<sup>[51,52,55-57]</sup> were also considered in this optimization. The vapor pressure of yttrium monoxide over a solid yttrium sesquioxides and the calculated vapor



**Fig. 5** Calculated isothermal section of Y-C-O ternary system at 1400 K along with experimental data<sup>[58]</sup>: (a) this work and (b) Ref 33



**Fig. 6** Calculated  $\text{SiO}_2\text{-SiC}$  vertical section in Si-C-O ternary system: (a) this work and (b) Ref 33

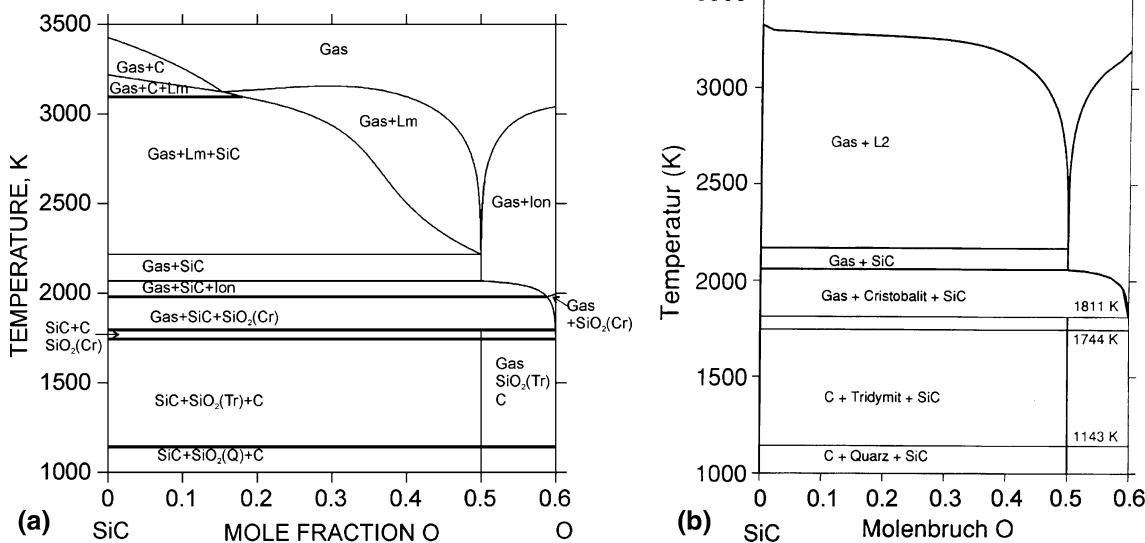
pressure of yttrium over the liquid containing unsaturating and saturating amounts of sesquioxide were calculated and compared with experimental data<sup>[51,52,55-57]</sup> (Fig. 3 and 4, respectively). The present calculations reproduce experimental data within uncertainty of measurements.

#### 4.2 Ternary Systems

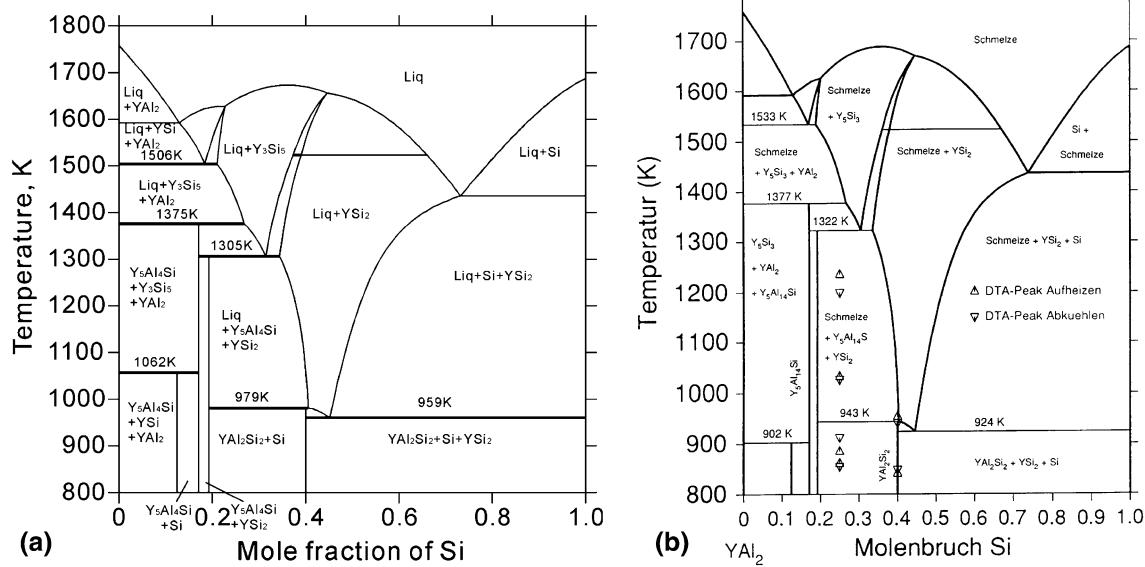
Nine ternary systems, Al-C-Si, Al-C-O, Al-C-Y, Al-O-Y, Al-Si-Y, C-Si-Y, C-O-Si, C-Y-O and O-Si-Y, were recalculated and compared with previous work of Gröbner.<sup>[33]</sup> The change of data for Y caused changes in the ternary system

Y-O-C, namely the homogeneity range of gamma ( $\gamma_2$ ) phase became very narrow thus conflicting with the experimental data of Brozek et al.<sup>[58]</sup> Ternary parameters of gamma phase in the Y-O-C system were adjusted to satisfy experimental data<sup>[58]</sup> (Fig. 5). It should be mentioned that tie-lines between  $\text{Y}_2\text{O}_3$ ,  $\gamma_2$ , C,  $\text{C}_2\text{Y}_3$ , and  $\text{C}_2\text{Y}$  phases calculated with present description are in agreement with experimental results<sup>[58]</sup> contrary to previous description of Gröbner.<sup>[33]</sup>

Several differences in ternary phase diagrams calculated using the present description and in work of Gröbner<sup>[33]</sup> can be explained by calculation problems arising due to the use of the older TC version by Gröbner.<sup>[33]</sup> For example, from a



**Fig. 7** Calculated section SiC-O: (a) present work and (b) Ref 33



**Fig. 8** Calculated section YAl<sub>2</sub>-Si: (a) present work and (b) Ref 33

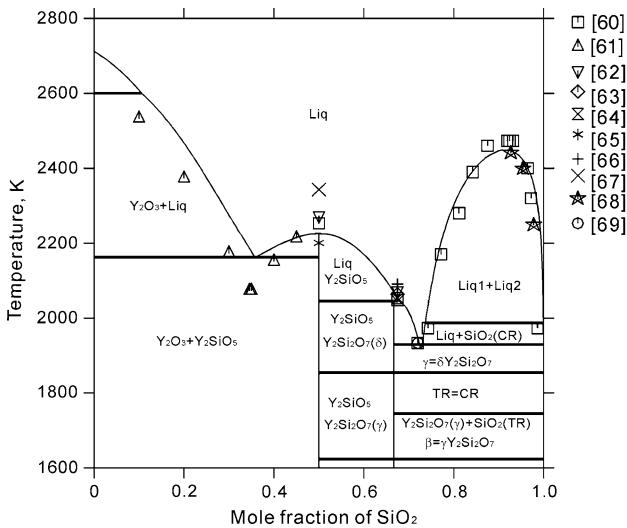
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comparison of the  $\text{SiO}_2$ - $\text{SiC}$  isopleths of the Si-C-O system presented in Fig. 6(a) with the work of Gröbner<sup>[33]</sup> (Fig. 6b) it can be concluded that problems at high temperature are now resolved. Another example for the  $\text{SiC}$ -O isopleths can be found in Fig. 7(a) and (b).

Some temperatures of invariant equilibrium changed because parameters of binary compounds in binary systems were changed. For example, in the  $\text{YAl}_2$ -Si vertical section of Y-Al-Si ternary system presented in Fig. 8(a) and (b), temperature of the heterogeneous reaction  $\text{Y}_3\text{Si}_5 + \text{YAl}_2 = \text{Y}_5\text{Al}_{14}\text{Si} + \text{YSi}$  is 1062 K according to calculations based on the present thermodynamic description and 902 K calculated by Gröbner.<sup>[33]</sup> In the same vertical section, difference in calculated temperatures between present work and Gröbner's<sup>[33]</sup> (shown in brackets, respectively) was indicated for several reactions, i.e.  $\text{Liq} + \text{YSi} = \text{Y}_3\text{Si}_5 + \text{YAl}_2$  (1506 and 1533 K),  $\text{YAl}_2\text{Si}_2 = \text{L} + \text{YSi}_2$  (979 and 943 K) and others. However, there are no experimental data for these invariant reactions and therefore parameters for the  $\text{Y}_5\text{Al}_{14}\text{Si}$ ,  $\text{YAl}_2\text{Si}_2$  phases or liquid were not re-optimized.

### **4.3 The $Y_2O_3-Al_2O_3-SiO_2$ System**

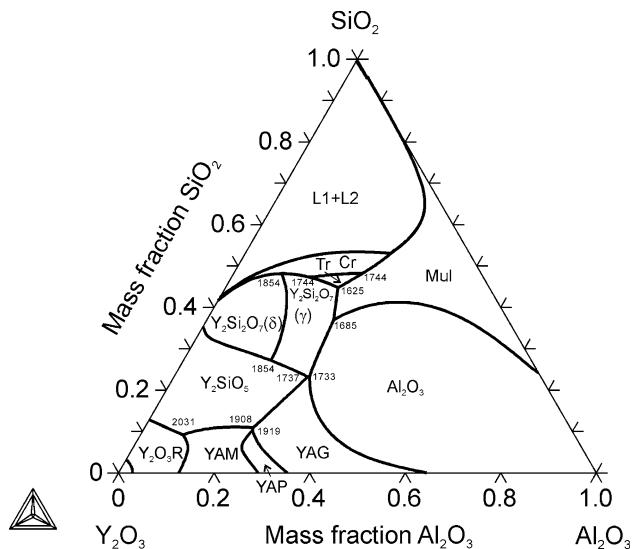
Thermodynamic description of  $\text{Y}_2\text{O}_3$ - $\text{Al}_2\text{O}_3$  binary system was taken from Fabrichnaya et al.<sup>[59]</sup> The thermodynamic parameters for the liquid phase in the  $\text{Y}_2\text{O}_3$ - $\text{SiO}_2$  ternary system was re-optimized in present work. The calculated phase diagram is shown in Fig. 9 along with experimental data.<sup>[60-69]</sup> Thermodynamic parameters for the YAM and liquid phases in the  $\text{Y}_2\text{O}_3$ - $\text{Al}_2\text{O}_3$ - $\text{SiO}_2$  ternary system were re-optimized using experimental data<sup>[70,71]</sup> and phase diagrams were recalculated. Liquidus surface calculated with the new description is presented in Fig. 10. The temperatures and liquid compositions of invariant reactions calculated with the new description are presented in comparison with experimental data and calculations of Mao et al.<sup>[30]</sup> in Table 1.



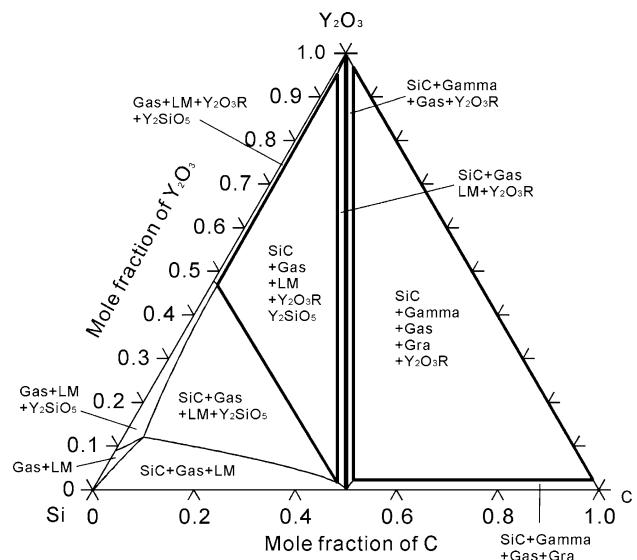
**Fig. 9** Calculated phase diagram of the  $\text{Y}_2\text{O}_3$ - $\text{SiO}_2$  system

#### **4.4 SiC-Y<sub>2</sub>O<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub>-SiO<sub>2</sub> System**

**4.4.1  $\text{Y}_2\text{O}_3$ -SiC.** To investigate the effect of carbon content on phase equilibria, the  $\text{Y}_2\text{O}_3$ -Si-C section in the Si-C-Y-O system was calculated at 2173 K (Fig. 11). Gas was always found to be in equilibrium with the condensed phases when 0.01 mole fraction of Ar was appended to the system. No ionic liquid was found stable at 2173 K in present calculations, because the temperature is much below the melting point of  $\text{Y}_2\text{O}_3$ . According to calculations, liquid metal forms when the carbon content is less than that along the  $\text{SiC}$ - $\text{Y}_2\text{O}_3$  line, while at higher carbon contents, gamma and graphite phases form.



**Fig. 10** The calculated liquidus surface of the  $\text{Al}_2\text{O}_3\text{-Y}_2\text{O}_3\text{-SiO}_2$  system; unit of temperature in this phase diagram is K



**Fig. 11** Calculated isothermal section of the Si-C-Y<sub>2</sub>O<sub>3</sub> system at 2173 K

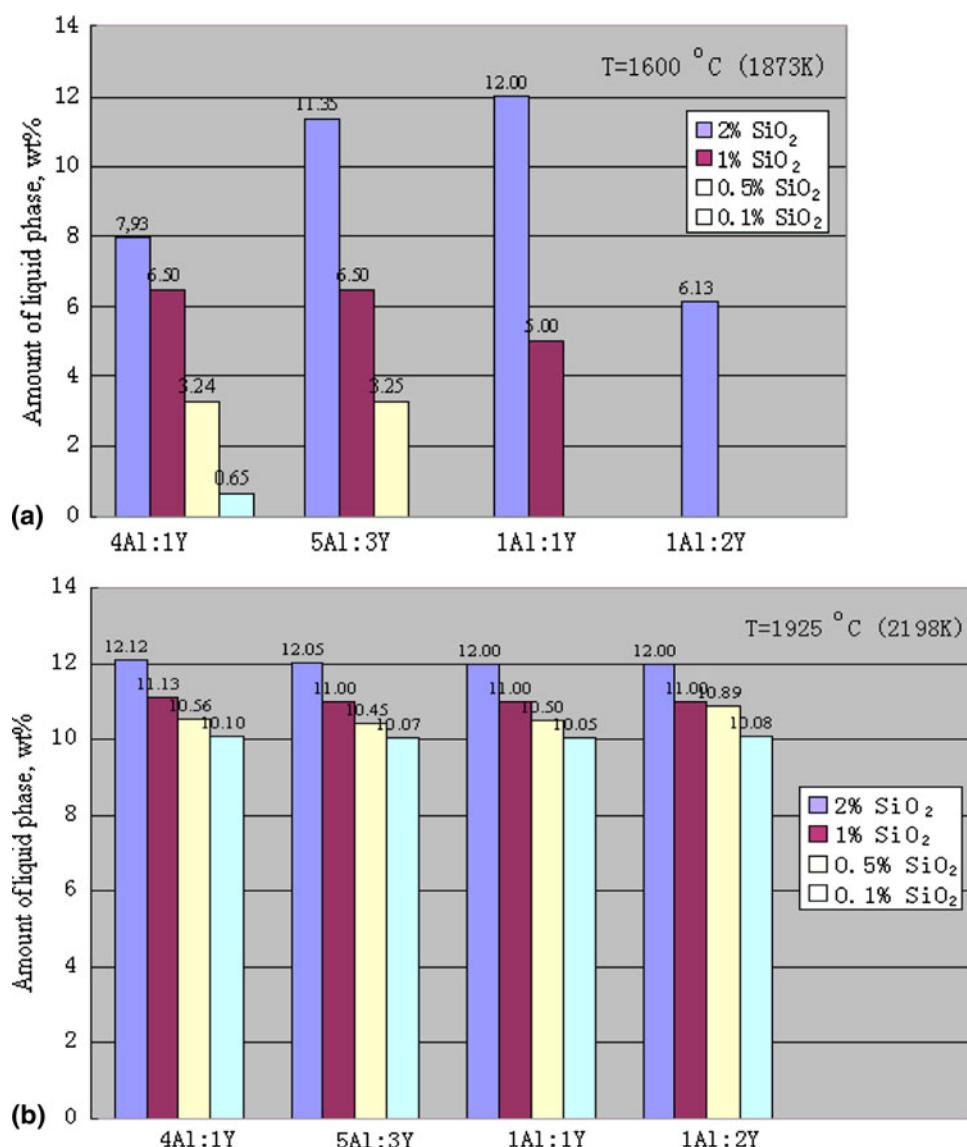
These calculations show that the expected compositions strongly depend on the carbon activity. This is in agreement with previous experimental results.<sup>[22]</sup>

**4.4.2 SiC-Y<sub>2</sub>O<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub>-SiO<sub>2</sub>.** Using the dataset re-assessed in this work, influence of Al<sub>2</sub>O<sub>3</sub> and Y<sub>2</sub>O<sub>3</sub> as additives in SiC liquid phase sintering was investigated by calculations and compared with experimental data. Since SiO<sub>2</sub> is always present as a surface layer on the SiC powder, the system as SiC-Y<sub>2</sub>O<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub>-SiO<sub>2</sub> was considered. Taking into account that most of the SiO<sub>2</sub> decomposes during sintering<sup>[72]</sup> the calculation of the SiO<sub>2</sub> free composition is also important.

The calculations were carried out without consideration of SiC solubility in the liquid phase.

According to calculations both the CO and SiO-partial pressures were highest in materials with large content of SiO<sub>2</sub>, which is consistent with work of Can et al.<sup>[72]</sup>

The calculated amount of the liquid phase formed for different Al<sub>2</sub>O<sub>3</sub>/Y<sub>2</sub>O<sub>3</sub> ratios and SiO<sub>2</sub> content at temperatures of 1600 and 1925 °C are presented in Fig. 12(a) and (b). Calculations at 1600 °C show the amount of liquid to have a maximum at Al<sub>2</sub>O<sub>3</sub>/Y<sub>2</sub>O<sub>3</sub> = 1 for the high SiO<sub>2</sub> content. It strongly decreases with decreasing SiO<sub>2</sub> content for all Al<sub>2</sub>O<sub>3</sub>/Y<sub>2</sub>O<sub>3</sub> ratios. For the Al<sub>2</sub>O<sub>3</sub>/Y<sub>2</sub>O<sub>3</sub> = 0.5 and SiO<sub>2</sub> content 1% and below no liquid forms according to calculations. Calculations at 1925 °C show a slight increase of liquid amount with increase of SiO<sub>2</sub> content and practically no dependence on the Al<sub>2</sub>O<sub>3</sub>/Y<sub>2</sub>O<sub>3</sub> ratio.



**Fig. 12** Calculated amount of liquid phase in a material with 10 wt.% additives depending on the Al<sub>2</sub>O<sub>3</sub>/Y<sub>2</sub>O<sub>3</sub> additive mole ratio at 1600 °C (a) and 1925 °C (b) for different SiO<sub>2</sub> contents (amount in wt.%) in the additives

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The phase relations in the sub-solidus region at 1400 °C (1673 K) calculated using the database derived in present study in absence of free oxygen and SiO<sub>2</sub> are compared with experimental results obtained by XRD investigation of annealed samples<sup>[73]</sup> in Table 3. The calculated results are in good agreement with the experimental data. Small amounts of the YAM phase (in samples YAlSiC-455510 and YAlSiC-455520) found in experiments are probably kinetically determined. Very small amounts of Al<sub>4</sub>SiC<sub>4</sub> (<0.34 wt.%) indicated by calculations for samples YAlSiC-604010, YAlSiC-604020, YAlSiC-802010 and YAlSiC-802050 were not detected experimentally in the microstructure nor by XRD. The reason of these small deviations is the reaction of SiC with YAM and Al<sub>2</sub>O<sub>3</sub> resulting in dissolution of the SiO<sub>2</sub> in YAM and formation of the Al<sub>4</sub>SiC<sub>4</sub> phase. The calculated isothermal section of the SiC-Y<sub>2</sub>O<sub>3</sub>-Al<sub>2</sub>O<sub>3</sub> system is presented in Fig. 13. It should be mentioned that graphite phase forms in the Y<sub>2</sub>O<sub>3</sub>-rich composition range in a very small amount ( $\sim 10^{-5}$ - $10^{-4}$  wt.%) and therefore this information is not presented in Table 3. Phase relations

were also calculated at high temperature (1850/1950 °C). The phase composition was in good agreement with the calculated data.

Temperatures of melting of the same compositions as in Table 3 were calculated assuming that the system does not contain SiO<sub>2</sub>. Comparison of melting temperatures of the same samples determined experimentally with calculated results (see Fig. 14) indicated reasonably good agreement in the Al<sub>2</sub>O<sub>3</sub>-rich compositions, while for the Y<sub>2</sub>O<sub>3</sub> rich compositions melting temperatures determined by STA (simultaneous thermal analysis) in Ref 67 are up to ~75 °C higher than obtained by calculation of phase equilibrium. The melting according to present calculations are accompanied by formation and dissolution of SiO<sub>2</sub> and a small amount of C in liquid phase as well as formation of Al<sub>4</sub>SiC<sub>4</sub>, and  $\gamma$ -phase depending on the composition. Metal liquid is indicated to form in all calculated mixtures. Formation of additional phases (Al<sub>4</sub>SiC<sub>4</sub> and  $\gamma$ -phases) depended only on Y<sub>2</sub>O<sub>3</sub>/Al<sub>2</sub>O<sub>3</sub> ratio but not on SiC content. Al<sub>4</sub>SiC<sub>4</sub> phase did not form in Al<sub>2</sub>O<sub>3</sub>-rich compositions. According to

**Table 3 Phase composition after preparation in SPS at 1400 °C (comparison between XRD and calculated results)**

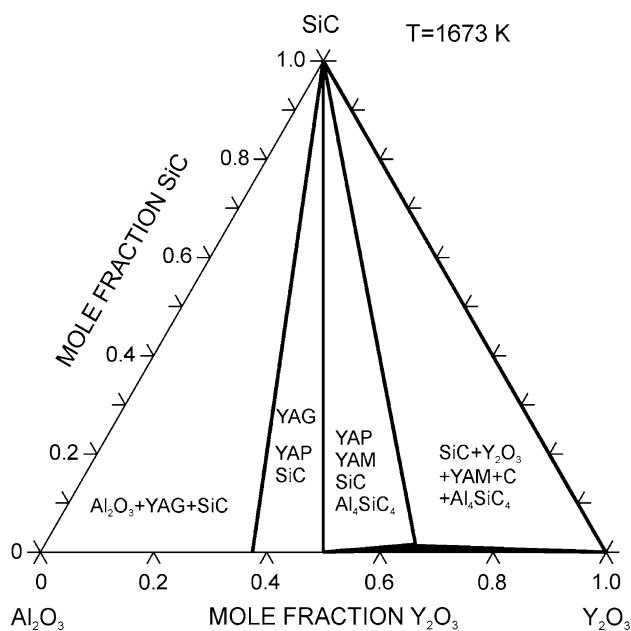
Sample/composition (mol%) Y <sub>2</sub> O <sub>3</sub> Al <sub>2</sub> O <sub>3</sub> SiC	SiC, wt.%	Al <sub>2</sub> O <sub>3</sub> , wt.%	YAG, wt.%	YAP, wt.%	YAM, wt.%	Y <sub>2</sub> O <sub>3</sub> , wt.%	Al <sub>4</sub> SiC <sub>4</sub> , wt.%	Residual Rwp, %
YAlSiC-208010								
18 72 10								
Experimental	3.8	38.6	57.7					6.5
Thermodyn. calculation	3.4	36.3	60.3					
YAlSiC-208020								
16 64 20								
Experimental	9	36.0	55.1					6.8
Thermodyn. calculation	7.3	34.8	57.9					
YAlSiC-455510								
40.5 49.5 10								
Experimental	2.5		35.4	57.2	4.9			6.1
Thermodyn. calculation	2.7		36.6	60.6				
YAlSiC-455520								
36 44 20								
Experimental	5.7		38.2	51.6	4.5			5.7
Thermodyn. calculation	6.0		35.4	58.6				
YAlSiC-604010								
54 36 10								
Experimental	1.9			42.5	55.7			6.1
Thermodyn. calculation	2.17			35.66	61.83	0.34		
YAlSiC-604020								
48 32 20								
Experimental	4.6			43.0	52.4			6.1
Thermodyn. calculation	5.09			34.60	59.98	0.33		
YAlSiC-802010								
72 18 10								
Experimental	3.5				52.6	44.0		7.3
Thermodyn. calculation	1.95				53.54	44.26	0.25	
YAlSiC-802050								
40 10 50								
Experimental	15.7				50.2	34.1		6.7
Thermodyn. calculation	16.44				45.63	37.72	0.21	

calculation, formation of  $\text{Al}_4\text{SiC}_4$  occurred for ratios of  $\text{Y}_2\text{O}_3/\text{Al}_2\text{O}_3$  equal to 45/55 and 60/40, in  $\text{Y}_2\text{O}_3$ -rich composition,  $\gamma$ -phase was forming. This interaction was not observed experimentally and could be the reason for the differences. The absence of experimental evidences for the interaction could be caused by kinetic reasons. The interaction is very slow or the formation of  $\text{SiO}_2$  could have a lower rate than the rate of evaporation of  $\text{SiO}_2$ . It should be mentioned that melting temperatures calculated in this

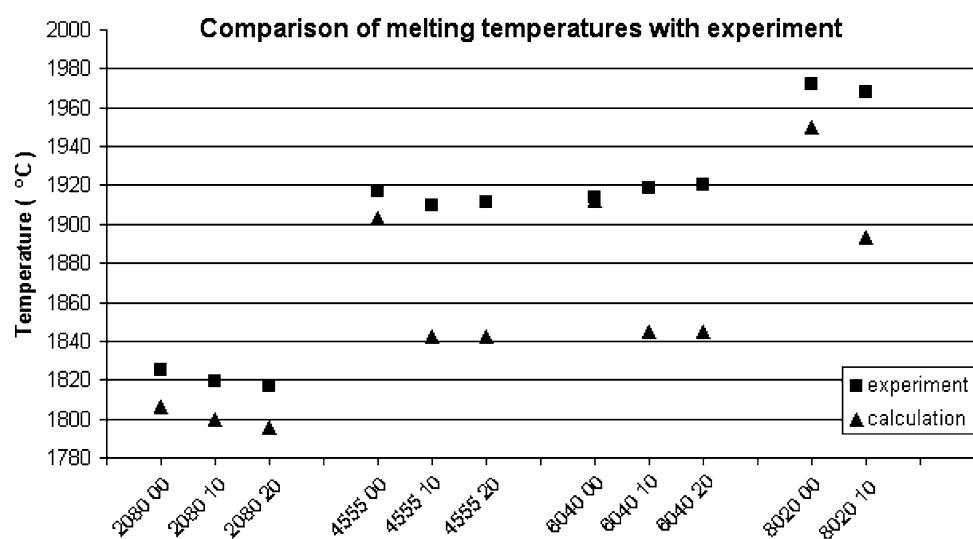
study for SiC-free samples were  $\sim 20$  °C lower than those determined in experiments.<sup>[73]</sup> This difference is quite acceptable taking into account higher uncertainty of experimental data used in optimization of the  $\text{Al}_2\text{O}_3\text{-Y}_2\text{O}_3$  system.<sup>[59]</sup> An additional reason for inconsistency could be that the thermodynamic model of the liquid does not include species of SiC. A next step for further improving of the thermodynamic model would be the introduction of SiC as neutral species in the model of liquid.

## 5. Conclusion

Taking into account the new description of yttrium, the database for the Si-C-Al-Y-O system was completely revised. The Y-O binary system was re-optimized in this work. For the optimization, phase diagram data and thermochemical properties of the different phases of the system were used. The parameters of the liquid phase in the  $\text{Y}_2\text{O}_3\text{-SiO}_2$  system were re-optimized in this work. In ternary system  $\text{Al}_2\text{O}_3\text{-Y}_2\text{O}_3\text{-SiO}_2$ , mixing parameters of YAM phase and ternary mixing parameters of liquid phase were re-optimized. Phase diagrams of  $\text{Al}_2\text{O}_3\text{-Y}_2\text{O}_3\text{-SiO}_2$ , and  $\text{SiC}\text{-Y}_2\text{O}_3\text{-SiO}_2$  systems were re-calculated and compared with earlier works. Phase diagram of the  $\text{SiC}\text{-Al}_2\text{O}_3\text{-Y}_2\text{O}_3$  systems was calculated at 1400 °C using updated description. Influence of  $\text{SiO}_2$  content and  $\text{Al}_2\text{O}_3/\text{Y}_2\text{O}_3$  ratio on amount of liquid forming at 1600 and 1925 °C was investigated using computational thermodynamics. Phase amounts calculated using an updated thermodynamic description of the  $\text{SiC}\text{-Al}_2\text{O}_3\text{-Y}_2\text{O}_3$  system indicated good agreement with experimentally studied compositions. However, comparison of melting temperatures of the same samples studied experimentally with calculated results reveals lower temperature of melting especially for the  $\text{Y}_2\text{O}_3$  rich compositions.



**Fig. 13** Calculated isothermal section the  $\text{SiC}\text{-Al}_2\text{O}_3\text{-Y}_2\text{O}_3$  system at 1400 °C



**Fig. 14** Comparison of melting temperatures determined experimentally in work of Ref 73 with calculations performed in the present study

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